Arithmetic laws

Answer Key

There are three laws of arithmetic that can be powerful tools to help with calculations.

1. Commutative laws

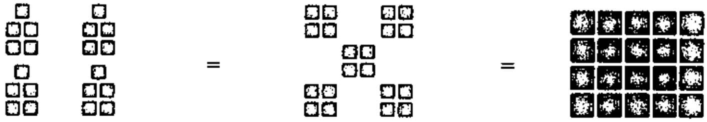
The order that we add or multiply numbers can be switched without changing the answer.

- Addition $a + b = b + a$

4 and 5 = 5 and 4

$4 + 5 = 5 + 4 = 9$

- Multiplication $a \times b = b \times a$



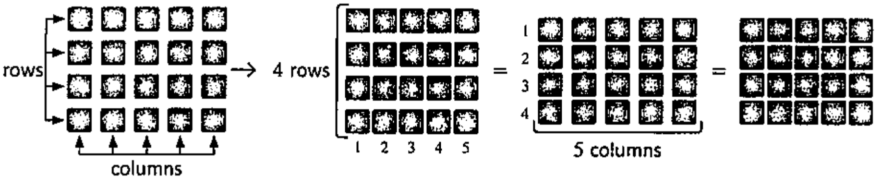
4 lots of 5 = 5 lots of 4

$4 \times 5 = 5 \times 4 = 20$

The commutative law for multiplication can be shown also in terms of rows and columns.

rows × *columns* = *columns* × *rows*

4 rows of 5 | 5 columns of 4



$4 \times 5 = 5 \times 4 = 20$

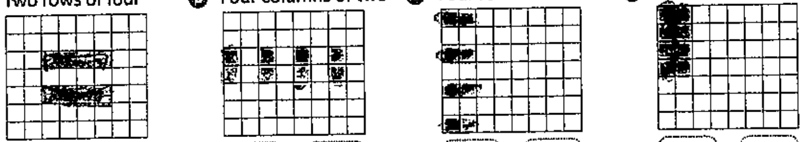
The commutative law does not work for subtraction or division as the order of the terms is important.

- $4 - 5 \neq 5 - 4 \rightarrow 4 - 5 = -1$ and $5 - 4 = 1$
- $4 \div 5 \neq 5 \div 4 \rightarrow 4 \div 5 = 0.8$ and $5 \div 4 = 1.25$

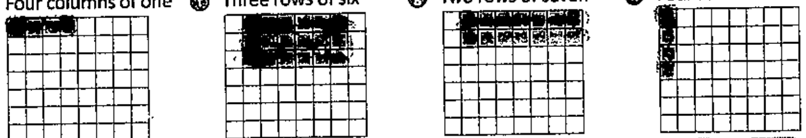
Commutative laws

1. Shade groups of boxes to match these descriptions and write the calculation they represent.

any position are ok



a. Two rows of four $= 2 \times 4$
b. Four columns of two $= 4 \times 2$
c. Four rows of two $= 4 \times 2$
d. Two columns of four $= 2 \times 4$



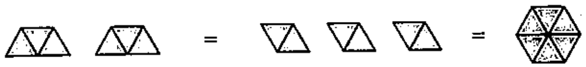
e. Four columns of one $= 4 \times 1$
f. Three rows of six $= 3 \times 6$
g. Two rows of seven $= 2 \times 7$
h. Four rows of one $= 4 \times 1$

2. Fill in the mathematical sentences for each of these diagrams showing the commutative law.

a.

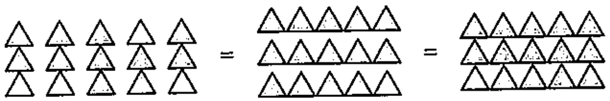
$3 + 2 = 2 + 3 = 5$

b.



$2 \times 3 = 3 \times 2 = 6$

c.



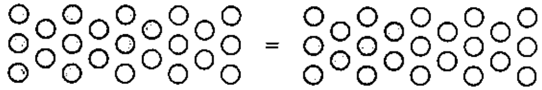
$5 \times 3 = 3 \times 5 = 15$

d.

$6 \times 3 = 3 \times 6 = 18$

Commutative laws

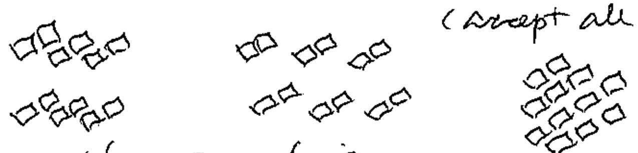
3. Write the expression for the commutative law represented by this diagram.



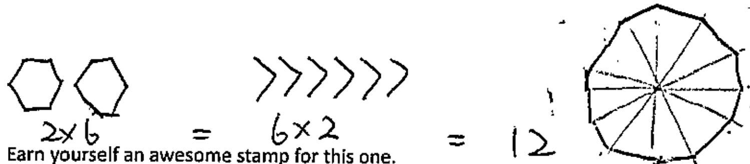
$13 + 10 = 10 + 13$

4. Draw two different diagrams below to demonstrate that $2 \times 6 = 6 \times 2 = 12$.

(accept all possible answers)



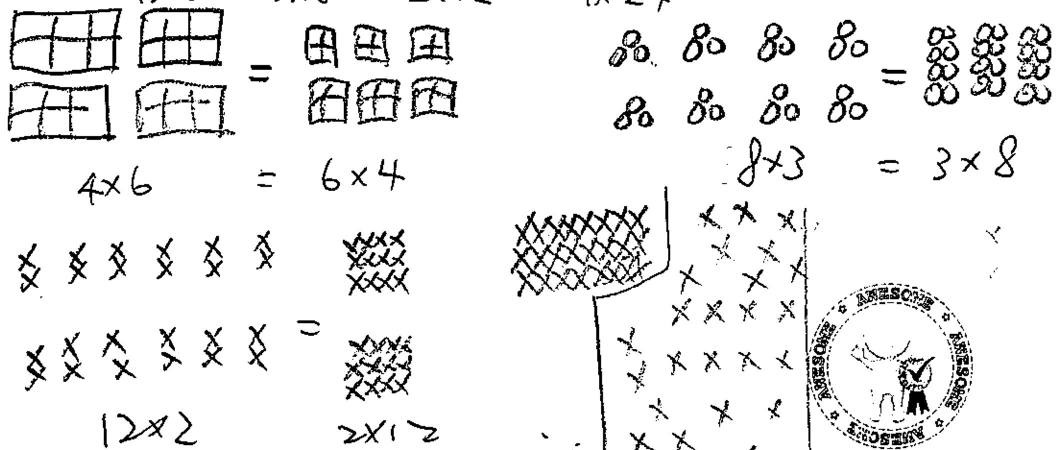
$2 \times 6 = 6 \times 2 = 12$



$2 \times 6 = 6 \times 2 = 12$

5. Earn yourself an awesome stamp for this one.
Draw all four different pairs of diagrams that represent the commutative law for multiplication with an answer of 24.

4×6 3×8 2×12 1×24



$4 \times 6 = 6 \times 4$

$8 \times 3 = 3 \times 8$

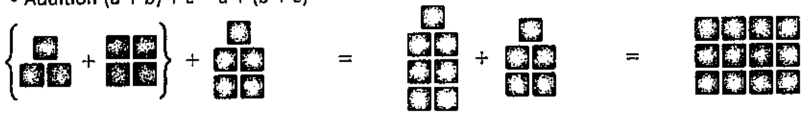
12×2 = 2×12

$1 \times 24 = 24 \times 1$

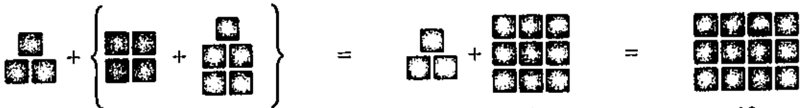
2. Associative laws

The numbers we group together when adding or multiplying can change without changing the answer.

- Addition $(a + b) + c = a + (b + c)$

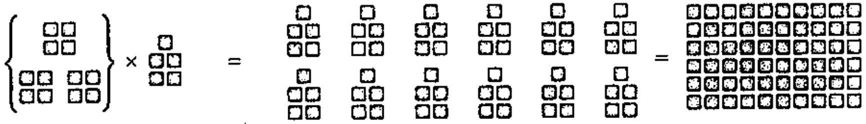


$(3 + 4) + 5 = 7 + 5 = 12$



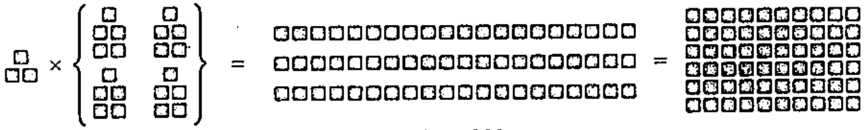
$3 + (4 + 5) = 3 + 9 = 12$

- Multiplication $(a \times b) \times c = a \times (b \times c)$



3 lots of 4 × 5 = 12 lots of 5 = 60

$(3 \times 4) \times 5 = 12 \times 5$



3 × 4 lots of 5 = 3 lots of 20 = 60

$3 \times (4 \times 5) = 3 \times 20$

The associative law can make adding/multiplying terms easier.

$31 + 25 + 9 = (31 + 9) + 25$
$= 40 + 25$
$= 65$

$13 \times 25 \times 4 = 13 \times (25 \times 4)$
$= 13 \times 100$
$= 1300$

What about subtraction or division?
There are only a few very special cases where the associative law works for subtraction and division.

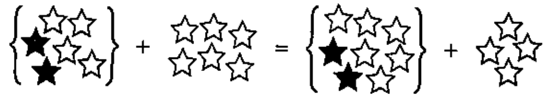
When a 0 is involved like this:
- $(6 - 2) - 0 = 6 - (2 - 0)$
- $(0 \div 7) \div 5 = 0 \div (7 \div 5)$

When a 1 is involved like this:
- $(18 \div 3) \div 1 = 18 \div (3 \div 1)$

In all other cases, the associative law does not work for subtraction and division.
- $(3 - 4) - 5 \neq 3 - (4 - 5) \rightarrow (3 - 4) - 5 = -6$ and $3 - (4 - 5) = 4$
- $(3 \div 4) \div 5 \neq 3 \div (4 \div 5) \rightarrow (3 \div 4) \div 5 = 0.15$ and $3 \div (4 \div 5) = 3.75$

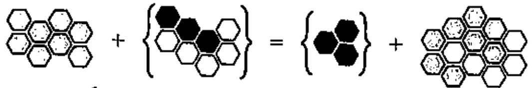
Associative laws

1. Complete these equations for the associative law of addition shown in each diagram.

a) 

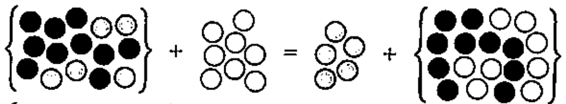
$\{2 + 4\} + 6 = \{2 + 6\} + 4$

$6 + 6 = 8 + 4 = 12$

b) 

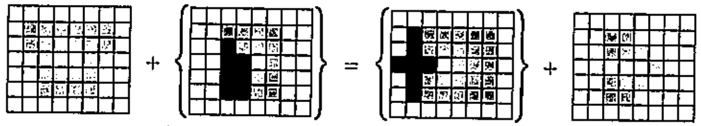
$8 + \{3 + 5\} = 3 + \{8 + 5\}$

$8 + 8 = 3 + 13 = 16$

c) 

$\{5 + 10\} + 8 = 5 + \{10 + 8\}$

$15 + 8 = 5 + 18 = 23$

d) 

$24 + \{7 + 13\} = \{7 + 24\} + 13$

$24 + 20 = 31 + 13 = 44$

Associative laws

The associative law lets us choose what we want to do first to make calculations easier and quicker.

For example:

$14 + 9 + 16$ is made easier by adding the 14 and 16 together first to make it $9 + 30 = 39$

Pairing up terms that make nicer whole numbers before adding to other terms is a great trick.

Use the associative law for addition to simplify these calculations:

a) $25 + 91 + 75 = \{\boxed{25} + \boxed{75}\} + 91$
$= \boxed{100} + 91$
$= \boxed{191}$

b) $83 + 52 + 18 = \{\boxed{52} + \boxed{18}\} + 83$
$= \boxed{70} + 83$
$= \boxed{153}$

c) $122 + 163 + 37 = \{\boxed{163} + \boxed{37}\} + \boxed{122}$
$= \boxed{200} + \boxed{122}$
$= \boxed{322}$

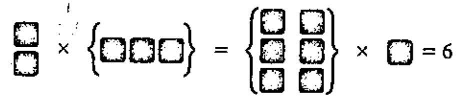
d) $102 + 43 + 25 = \{\boxed{102} + \boxed{43}\} + \boxed{25}$
$= \boxed{145} + \boxed{25}$
$= \boxed{170}$

e) $37 + 14 + 56 + 23 = (37+23)+(14+56)$
$= 60+70$
$= 130$

f) $111 + 80 + 19 + 45 = (111+19)+(80+45)$
$= 130+125$
$= 255$

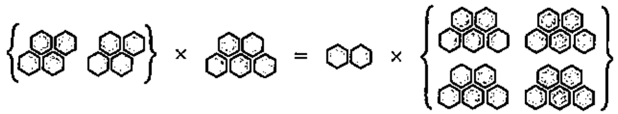
Associative laws

Complete these equations for the associative law of multiplication shown in each diagram.

a) 

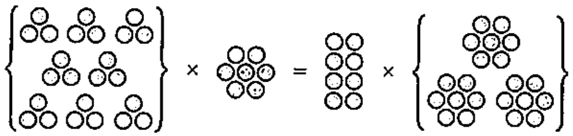
$\boxed{2} \times \{\boxed{3} \times \boxed{1}\} = \{\boxed{2} \times \boxed{3}\} \times \boxed{1}$

$\boxed{2} \times \boxed{3} = \boxed{6} \times \boxed{1} = 6$

b) 

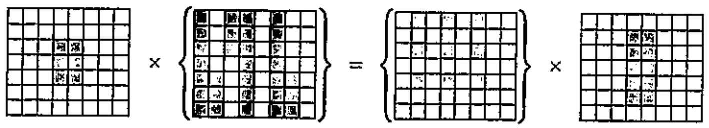
$\{\boxed{2} \times \boxed{4}\} \times \boxed{5} = \boxed{2} \times \{\boxed{4} \times \boxed{5}\}$

$\boxed{8} \times \boxed{5} = \boxed{2} \times \boxed{20} = 40$

c) 

$\{\boxed{8} \times \boxed{3}\} \times \boxed{7} = \boxed{8} \times \{\boxed{3} \times \boxed{7}\}$

$\boxed{24} \times \boxed{7} = \boxed{8} \times \boxed{21} = 168$

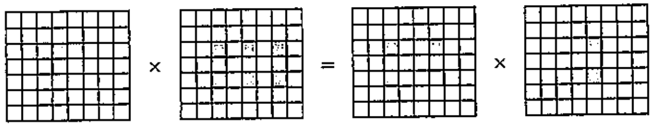
d) 

$\boxed{6} \times \{\boxed{3} \times \boxed{10}\} = \{\boxed{6} \times \boxed{3}\} \times \boxed{10}$

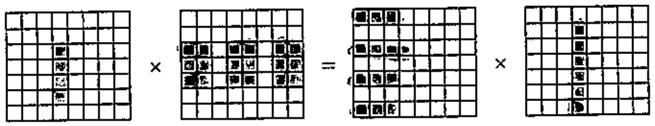
$\boxed{6} \times \boxed{30} = \boxed{18} \times \boxed{10} = \boxed{180}$

Associative laws

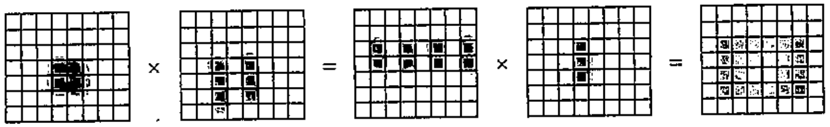
4. Shade groups of squares in these grids to match the associative law of multiplication underneath.

a) 

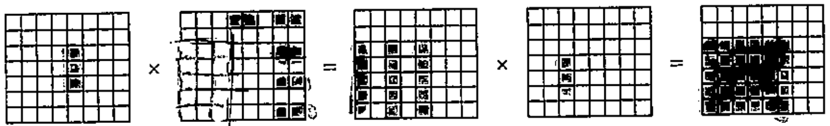
2 × (3 × 3) = (2 × 3) × 3

b) 

4 × (3 × 6) = (4 × 3) × 6

c) 

4 × (2 × 3) = (4 × 2) × 3 = 24

d) 

3 × (5 × 2) = (3 × 5) × 2 = 30

5. Use the associative law for multiplication to simplify these calculations:

a) 5 × 28 × 20 = {5 × 20} × 28
= 100 × 28
= 2800

b) 12 × 50 × 7 = {12 × 50} × 7
= 600 × 7
= 4200

c) 4 × 9 × 75 = {4 × 75} × 9
= 300 × 9
= 2700

d) 15 × 12 × 11 = {15 × 12} × 11
= 180 × 11
= 1980

Associative laws

6. Tick the box 'true' or 'false' to show which of these subtraction or division statements are special cases where the associative law does work.

a) (12 ÷ 4) ÷ 1 = 12 ÷ (4 ÷ 1) ☑ True ☐ False
b) (5 ÷ 0) ÷ 3 = 5 ÷ (0 ÷ 3) ☐ True ☑ False
c) (0 − 4) − 3 = 0 − (4 − 3) ☐ True ☑ False
d) (0 ÷ 16) ÷ 2 = 0 ÷ (16 ÷ 2) ☑ True ☐ False
e) (20 − 11) − 0 = 20 − (11 − 0) ☑ True ☐ False
f) (5 ÷ 1) ÷ 5 = 5 ÷ (1 ÷ 5) ☐ True ☑ False
g) (0 ÷ 1) ÷ 1 = 0 ÷ (1 ÷ 1) ☑ True ☐ False
h) (8 − 0) − 1 = 8 − (0 − 1) ☐ True ☑ False
i) (1 − 1) − 1 = 1 − (1 − 1) ☐ True ☑ False
j) (0 − 1) − 0 = 0 − (1 − 0) ☑ True ☐ False

7. Larger strings of numbers can also have the associative law applied to them.

Group terms together in these expressions that make the calculation much easier.

a) 12 + 34 + 8 + 4 + 2
(12+8)+(34+4+2)
= 20 + 40
= 60

Explain why you grouped the numbers you did.

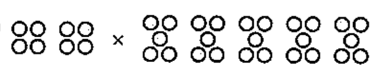
they become multiple of 10.

b) 12 × 2 × 5 × 3
(2×5)×(12×3)
= 10 × 36
= 360

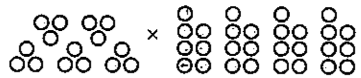
c) Use the associative law to rearrange into three pairs to make the calculation easier.

23 + 11 + 37 + 24 + 16 + 9
= (23+37)+(11+9)+(24+16)
= 60 + 20 + 40 = 120

8. Write an expression that represents these dot diagrams and use the associative law to simplify.

a) 

2×4 × 5×5
= (2×5)×(4×5)
= 10×20
= 200

b) 

5×3 × 4×7
= (5×4)×(3×7)
= 20 × 21
= 420

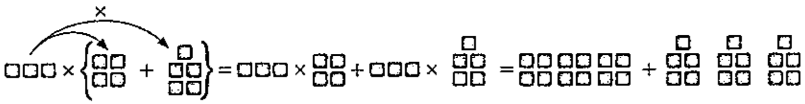
3. Distributive law

This law allows you to spread a multiplication out (or expand) into smaller parts to make it simpler.

- Using the order of operations and calculating the brackets first:

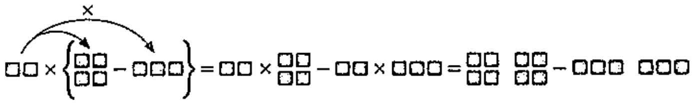
$3 \times (4 + 5) = 3 \times (9) = 27$

- Distributing the multiplication to each term within the brackets:



$3 \times (4 + 5) = 3 \times 4 + 3 \times 5 = 12 + 15 = 27$

Also works if a subtraction is inside the brackets.



$2 \times (4 - 3) = 2 \times 4 - 2 \times 3 = 8 - 6 = 2$

So the distributive law is:

$a \times (b + c) = a \times b + a \times c$

These signs must always match

$a \times (b - c) = a \times b - a \times c$

These signs must always match

Using this law in reverse makes the multiplication of large numbers easy to calculate mentally.

For example, we can use the distributive law to calculate 127×4 using either of these:

$120 \times 4 + 7 \times 4$ or $130 \times 4 - 3 \times 4$

$$\begin{aligned}127 \times 4 &= (120 + 7) \times 4\\ &= 120 \times 4 + 7 \times 4\\ &= 480 + 28\\ &= 508\end{aligned}$$

$$\begin{aligned}127 \times 4 &= (130 - 3) \times 4\\ &= 130 \times 4 - 3 \times 4\\ &= 520 - 12\\ &= 508\end{aligned}$$

You could have split 127 up into any sum/subtraction you found easiest to use.

Distributive law

1. Fill in the missing values for each of these examples of the distributive law.

a) $3 \times \{5 + \boxed{6}\} = 3 \times \boxed{5} + 3 \times 6$

b) $\boxed{7} \times \{8 - 4\} = 7 \times 8 - 7 \times \boxed{4}$

c) $6 \times 13 + 6 \times 9 = \boxed{6} \times \{\boxed{13} + \boxed{9}\}$

d) $\boxed{15} \times 7 - \boxed{15} \times 10 = 15 \times \{7 - \boxed{10}\}$

e) $\boxed{5} \times \{9 + \boxed{11}\} = 45 + 5 \times 11$

f) $12 \times \{\boxed{3} - \boxed{1}\} = 36 - 12$

2. a) Use the distributive law to expand these multiplications:

α) $5 \times \{8 + 2\} = 5 \times \boxed{8} + 5 \times \boxed{2} = \boxed{40} + \boxed{10} = \boxed{50}$

β) $5 \times \{4 + 6\} = 5 \times \boxed{4} + 5 \times \boxed{6} = \boxed{20} + \boxed{30} = \boxed{50}$

b) Explain why both have the same value even though the terms in the brackets are different.

The sum inside both brackets are the same

c) Write another similar expression to those in a) that will also give the same answer.

$5 \times \{0 + 10\}$, $5 \times (3 + 7)$, $5 \times (1 + 9)$, $5(5 + 5)$

3. Use the distributive law to simplify and evaluate these multiplications:

a) $6 \times 25 = 6 \times \{\boxed{20} + \boxed{5}\} = 6 \times \boxed{20} + 6 \times \boxed{5} = \boxed{120} + \boxed{30} = \boxed{150}$

b) $8 \times 98 = 8 \times \{\boxed{100} - \boxed{2}\} = 8 \times \boxed{100} - 8 \times \boxed{2} = \boxed{800} - \boxed{16} = \boxed{784}$

c) $11 \times 32 = 11 \times \{\boxed{30} + \boxed{2}\} = 11 \times \boxed{30} + 11 \times \boxed{2} = \boxed{330} + \boxed{22} = \boxed{352}$

d) $15 \times 19 = 15 \times \{\boxed{20} - \boxed{1}\} = 15 \times \boxed{20} - 15 \times \boxed{1} = \boxed{300} - \boxed{15} = \boxed{285}$

Distributive law

You can apply the distributive law more than once to simplify a calculation:

For example:

$$25 \times 59 = 25 \times (60 - 1)$$
$$= 25 \times 60 - 25 \times 1$$
$$= 25 \times 60 - 25$$

$$= (20 + 5) \times 60 - 25$$
$$= 20 \times 60 + 5 \times 60 - 25$$
$$= 1200 + 300 - 25$$
$$= 1475$$

OR

$$= 25 \times 60 - 25$$
$$= 25 \times (20 + 40) - 25$$
$$= 25 \times 20 + 25 \times 40 - 25$$
$$= 500 + 1000 - 25$$
$$= 1475$$

(Accept reasonable answer)

Apply the distributive law twice to simplify and calculate these:

a) $14 \times 37 = 14 \times (40 - 3)$
$= 14 \times 40 - 14 \times 3$
$= (10 + 4) \times 40 - 42$
$= 10 \times 40 + 4 \times 40 - 42$
$= 400 + 160 - 42$
$= 560 - 42$
$= 518$

b) $45 \times 82 = 45 \times (80 + 2)$
$= 45 \times 80 + 45 \times 2$
$= (40 + 5) \times 80 + 90$
$= 40 \times 80 + 80 \times 5 + 90$
$= 3200 + 400 + 90$
$= 3690$

c) 22×75
$= 22 \times (70 + 5)$
$= 22 \times 70 + 22 \times 5$
$= (20 + 2) \times 70 + 110$
$= 20 \times 70 + 2 \times 70 + 110$
$= 1400 + 140 + 110 = 1650$

d) 25×112
$= 25 \times (100 + 12)$
$= 25 \times 100 + \cancel{25 \times 12}$
$= 2500 + (20 + 5) \times 12$
$= 2500 + 20 \times 12 + 5 \times 12$
$= 2500 + 420 + 60 = 2800$

e) $83 \times 35 = 35 \times (80 + 3)$
$= 35 \times 80 + 35 \times 3$
$= (30 + 5) \times 80 + 105$
$= 30 \times 80 + 5 \times 80 + 105$
$= 2400 + 400 + 105$
$= 2905$

f) $120 \times 108 = 120 \times (110 - 2)$
$= 120 \times 110 - 120 \times 2$
$= (100 + 20) \times 110 - 240$
$= 11000 + 2200 - 240$
$= 12960$

Factor trees

Composite numbers can be divided exactly (with no remainder), by other smaller or equal whole numbers called **factors.**

Composite numbers:	15	9	12	4	24
Factors:	1, 3, 5, 15	1, 3, 9	1, 2, 3, 4, 6, 12	1, 2, 4	1, 2, 3, 4, 6, 8, 12, 24

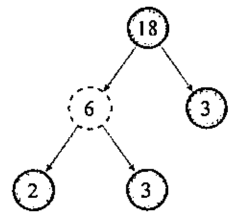
Prime numbers only have 1 and themself as factors.

Prime numbers:	2	3	17	11	31
Factors:	1, 2	1, 3	1, 17	1, 11	1, 31

All composite numbers can be written as the product (×) of **prime factors** (all the prime numbers that divide exactly into them). Let's see how.

'Express' is a another way of saying 'write' in Mathematics.

Express 18 as a product of its prime factors



Split 18 into two smaller factors

Solid circle around prime numbers to stop that branch

Split 6 into two smaller factors

Solid circle around prime numbers to stop that branch

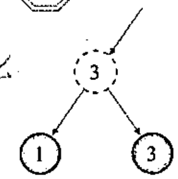
Once every branch has reached a prime number, multiply all the prime numbers together

$$\therefore 18 = 2 \times 3 \times 3$$
$$= 2 \times 3^2$$

Simplify answer

ALWAYS STOP at the prime number.

Don't ever do this

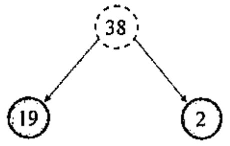


because 1 is NOT a prime number

Remember:
A prime number has two factors, itself and 1

Here are some more examples.

Express 38 as a product of its prime factors



Split 38 into two smaller factors

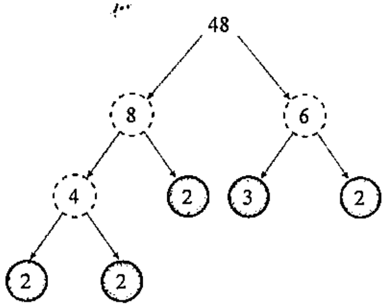
Solid circle around prime numbers to stop that branch

Once every branch has reached a prime number, multiply all the prime numbers together

$\therefore 38 = 19 \times 2$

There is often more than one way to create a factor tree for numbers with a lot of factors.

Express 48 as a product of its prime factors



Split 48 into two smaller factors

Split 6 and 8 into two smaller factors

Solid circle around prime numbers to stop that branch
Split 4 into two smaller factors

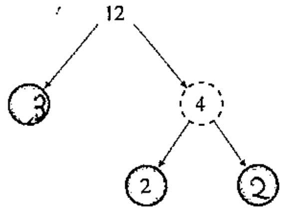
Solid circle around prime numbers to stop that branch

Once every branch has reached a prime number, multiply all the prime numbers together

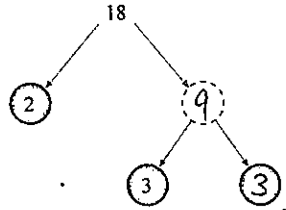
$\therefore 48 = 2 \times 2 \times 2 \times 3 \times 2$
$= 2^4 \times 3$ Simplify answer

Factor trees

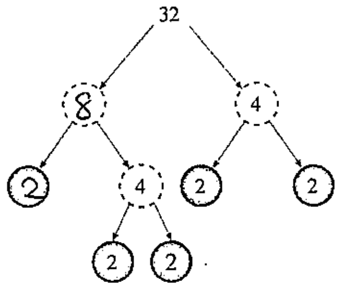
13. Fill in the missing values on the following factor trees and write the number as a product of its primes.

a) 

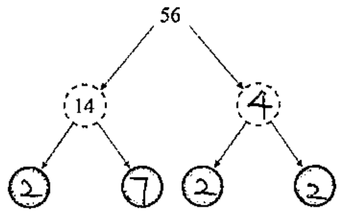
$\therefore 12 = 2 \times 2 \times 3$
$= 2^2 \times 3$

b) 

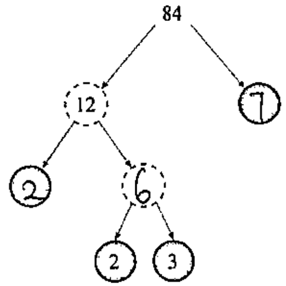
$\therefore 18 = 2 \times 3 \times 3 = 2 \times 3^2$

c) 

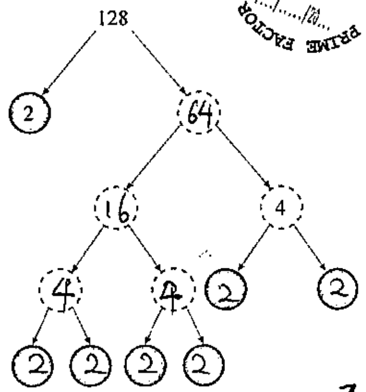
$\therefore 32 = 2 \times 2 \times 2 \times 2 \times 2 = 2^5$

d) 

$\therefore 56 = 2 \times 2 \times 2 \times 7$
$= 2^3 \times 7$

e) 

$\therefore 84 = 2 \times 2 \times 3 \times 7$
$= 2^2 \times 3 \times 7$

f) 

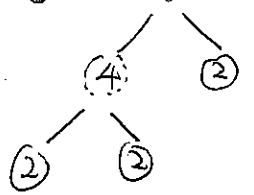
$\therefore 128 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 2^7$

Factor trees

2. Complete a factor tree for each number below and express them as a product of their prime factors.

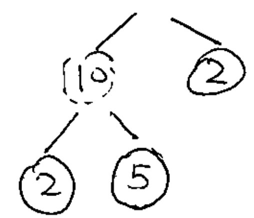
accept reasonable answer

a) 8



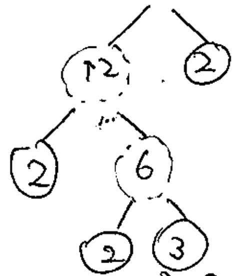
$\therefore 8 = 2^3$

b) 20



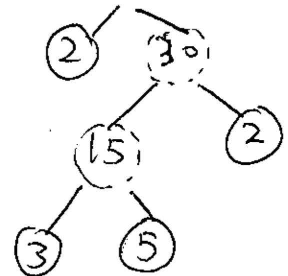
$\therefore 20 = 2 \times 2 \times 5 = 2^2 \times 5$

c) 24



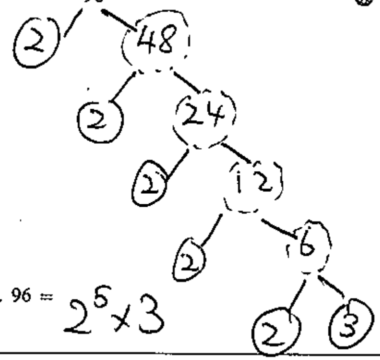
$\therefore 24 = 2^3 \times 3$

d) 60



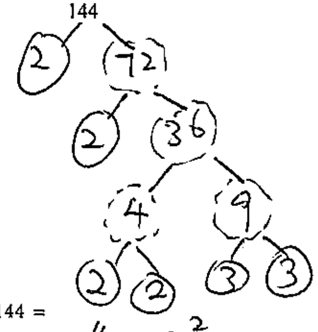
$\therefore 60 = 2^2 \times 3 \times 5$

e) 96



$\therefore 96 = 2^5 \times 3$

f) 144



$\therefore 144 = 2^4 \times 3^2$

Highest common factor (HCF)

The HCF is the largest number that divides exactly into two or more composite numbers.

Write all the factors of each number then circle the largest one which appears in both lists.

Find the highest common factor for these pairs of numbers

(i) 6 and 8

Factors of 6: 1 , 2 , 3 , 6 — List all the factors for each number

Factors of 8: 1 , 2 , 4 , 8 — Circle the largest number common to both lists

∴ The HCF for 6 and 8 is: **2**

(ii) 18 and 12

Factors of 18: 1 , 2 , 3 , 6 , 9 , 18 — List all the factors for each number

Factors of 12: 1 , 2 , 3 , 4 , 6 , 12 — Circle the largest number common to both lists

∴ The HCF for 18 and 12 is: **6**

We can use the list of prime factors for larger numbers to find the HCF.

Find the HCF for these pairs of larger numbers

(i) 72 and 96

Factors of 72: 2 , 2 , 2 , 3 , 3 — List all the **prime** factors for each number

Factors of 96: 2 , 2 , 2 , 2 , 2 , 3

∴ The HCF for 72 and 96 is: $2 \times 2 \times 2 \times 3 = 24$

(ii) 528 and 624

Factors of 528: 2 , 2 , 2 , 2 , 3 , 11 — List all the **prime** factors for each number

Factors of 624: 2 , 2 , 2 , 2 , 3 , 13

∴ The HCF for 528 and 624 is: $2 \times 2 \times 2 \times 2 \times 3 = 48$

Highest common factor (HCF)

1 Find the highest common factor for these pairs of numbers.

a 8 and 12

Factors of 8 : 1, 2, 4, 8
Factors of 12 : 1, 2, 3, 4, 6, 12
∴ The H.C.F for 8 and 12 is: 4

b 6 and 15

6 : 1, 2, 3, 6
15 : 1, 3, 5, 15
∴ The H.C.F of 6 and 15 is 3.

c 10 and 18

10 : 1, 2, 5, 10
18 : 1, 2, 3, 6, 9, 18
∴ the H.C.F is 2

d 18 and 24

18 = 1, 2, 3, 6, 9, 18
24 : 1, 2, 3, 4, 6, 8, 12, 24
∴ the H.C.F. is 6

e 14 and 28

14 ; 1, 2, 7, 14
28 ; 1, 2, 4, 7, 14, 28
∴ The H.C.F. is 14

f 16 and 36

16 = 1, 2, 4, 8, 16
36 = 1, 2, 3, 4, 6, 9, 12, 36
∴ The H.C.F. is 4

2 Use the prime factors to find the HCF for these larger numbers.

a 42 and 84

$42 = 2 \times 2 \times 2 \times 2 \times 3$
$84 = 2 \times 2 \times 3 \times 7$
∴ H.C.F. $= 2 \times 2 \times 3 = 12$

b 92 and 72

$92 = 2 \times 2 \times 23$
$72 = 2 \times 2 \times 2 \times 3 \times 3$
∴ H.C.F. $= 2 \times 2 = 4$

c 280 and 490

$280 = 2 \times 2 \times 2 \times 5 \times 7$
$490 = 2 \times 5 \times 7 \times 7$
∴ H.C.F $= 2 \times 5 \times 7$
$= 70$

d 256 and 640

$256 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2$
$640 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 5$
∴ H.C.F. $= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2$
$= 128$

Lowest common multiple (LCM)

The LCM is the smallest number that is common to the multiplication tables of two or more numbers.

Write down the multiples of the numbers and stop once you find the lowest common multiple.

Find the lowest common multiple for these pairs of numbers

(i) 2 and 5

Multiples of 2: $\underset{1\times2}{2}$, $\overset{2\times2}{4}$, $\underset{3\times2}{6}$, $\overset{4\times2}{8}$, $\underset{5\times2}{10}$, $\overset{6\times2}{12}$, $\underset{7\times2}{14}$,... List some multiples of the first number

Multiples of 5: $\underset{1\times5}{5}$, $\overset{2\times5}{10}$,... List the multiples of the second number until there is a match

∴ The LCM for 2 and 5 is: **10**

(ii) 6 and 8

Multiples of 6: 6 , 12 , 18 , 24 , 30 ,... List some multiples of the first number

Multiples of 8: 8 , 16 , 24 ,... List the multiples of the second number until there is a match

∴ The LCM for 6 and 8 is: **24**

We can use the list of prime factors for larger numbers to find the LCM by looking at the differences.

Find the LCM for these pairs of larger numbers

(i) 30 and 100

Prime factors of 30: 2 , 3 , 5 — List all the prime factors for both numbers

Prime factors of 100: 2 , 2 , 5 , 5 — Circle all the different factors in the smaller number

∴ The LCM for 30 and 100 is: $100 \times 3 = 300$ — Multiply the larger number by the different factor

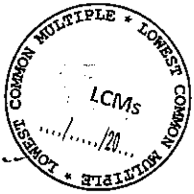
(ii) 24 and 388

Prime factors of 24: 2 , 2 , 2 , 3 — List all the prime factors for both numbers

Prime factors of 388: 2 , 2 , 97 — Circle all the different factors in the smaller number

∴ The LCM for 15 and 388 is: $388 \times 2 \times 3 = 2328$ — Multiply the larger number by the different factors

Lowest common multiple (LCM)



1. Find the lowest common multiple for these pairs of numbers.

a. 3 and 9

Multiples of 3 = 3, 6, 9 ...
Multiples of 9 = 9, 18, 27 ...

L.C.M = 9

b. 5 and 10

5 : 5, 10, 15, 20 ...
10 : 10, 20, 30 ...

L.C.M. = 10

c. 4 and 6

4, 8, 12, 16 ...
6, 12, 18, 24 ...

L.C.M = 12

d. 5 and 6

5, 10, 15, 20, 25, 30, 35 ...
6, 12, 18, 24, 30, 36 ...

L.C.M = 30

e. 6 and 7

6, 12, 18, 24, 30, 36, 42, 48 ...
7, 14, 21, 28, 35, 42, 49

L.C.M = 42

f. 12 and 16

12, 24, 36, 48, 60 ...
16, 32, 48, 64 ...

L.C.M = 48

2. Use the prime factors to find the LCM for these larger numbers.

a. 60 and 108

$60 = 2 \times 2 \times 3 \times 5$
$108 = 2 \times 2 \times 3 \times 3 \times 3$

$L.C.M = 2 \times 2 \times 3 \times 3 \times 3 \times 5$
$= 540$

b. 42 and 150

$42 = 2 \times 3 \times 7$
$150 = 2 \times 3 \times 5 \times 5$

$L.C.M = 2 \times 3 \times 5 \times 5 \times 7$
$= 150 \times 7 = 1050$

c. 168 and 180

$168 = 2 \times 2 \times 2 \times 3 \times 7$
$180 = 2 \times 2 \times 3 \times 3 \times 5$

$L.C.M = 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 7$
$= 8 \times 5 \times 9 \times 7$
$= 2520$

d. 210 and 385

$210 = 2 \times 3 \times 5 \times 7$
$385 = 5 \times 7 \times 11$

$L.C.M = 2 \times 3 \times 5 \times 7 \times 11$
$= 10 \times 21 \times 11$
$= 2310$